

ALGEBRA I EOC

REVIEW BOOK

Name: _____

Teacher's Name: _____

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1. Which of the following graphs represents exponential decay?



2. The amount of bacteria from the school water fountain is expected to double each week. Which equation can be used to represent this problem situation?

a. y = 2(.03)*	b. y = 4(2)
	- 1

c. $y = 3(\frac{1}{2})^x$ d. $y = 2(5)^x$

3. Which y-intercept and asymptote describes the exponential function below?

у -	+U(2)
a. y-intercept: 100	b, y- intercept 40
asymptote: y = 40	asymptote: y = ½
c. y-intercept: 100	d. y-intercept: 40
asymptote: x = 0	asymptote: y = 0
Construction of the second second	I I I I I I I I I I I I I I I I I I I

4. What is the domain and range for the exponential function below?



a. Domain: y > -1

Range: -∞ < x < ∞

c. Domain: -∞ ≤ x ≤ ∞ Range: y > -1 b. Domain: -∞ < x < ∞ Range: y ≥ -1

d. Domain: x > -1 Range: -∞ ≤ y ≤ ∞

Exponential Growth and Decay



Exponential Growth vs. Exponential Decay:



- GROWTH: when a > 0 and b > 1
- DECAY: when a > 0 and b is between 0 and 1.

KEY FEATURES:

 Every exponential graph has a horizontal asymptote (y =) that the graph will never cross.



-Horizontal asymptote: y = -4

-The graph will never touch or cross this line.

- Domain: -∞ ≤ x ≤ ∞ (all real numbers)
- Range: y > -4 **use the value from your asymptote**
 - o Since the graph never passes y = -4 you NEVER use ≥

STAAR ALGEBRA I REFERENCE MATERIALS

FACTORING	
Perfect square trinomials	$a^{2} + 2ab + b^{2} = (a + b)^{2}$ $a^{2} - 2ab + b^{2} = (a - b)^{2}$
Difference of squares	$a^2 - b^2 = (a - b)(a + b)$
PROPERTIES OF EXPONENTS	
Product of powers	$a^m a^n = a^{(m+n)}$
Quotient of powers	$\frac{a^m}{a^n} = a^{(m-n)}$
Power of a power	$(a^m)^n = a^{mn}$
Rational exponent	$a^{\frac{m}{n}} = \sqrt[\eta]{a^m}$
Negative exponent	$a^{-n}=\frac{1}{a^n}$
LINEAR EQUATIONS	
Standard form	Ax + By = C
Slope-Intercept form	y = mx + b
Point-slope form	$y-y_1=m(x-x_1)$
Slope of a line	$m = \frac{y_2 - y_1}{x_2 - x_1}$
QUADRATIC EQUATIONS	
Standard form	$f(x) = ax^2 + bx + c$
Vertex form	$f(x) = a(x-h)^2 + k$
Quadratic formula	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
Axis of symmetry	$x = \frac{-b}{2a}$

Problem Solving Strategy

Question – <u>Underline</u> the question.

Data - Circle important words and numbers.

Plan – How should I answer this question?

Answer – Follow the plan.

Check- Does your answer make sense?



1. At what height did the diver begin?

2. When will the diver hit the water?

3. What is the maximum height the diver reached? When did she reach it?

4. Find the domain and range for this problem situation.

Quadratic Real World Application

Quadratic Transformations

Calculator Strategies

Quadratic Parent function: $f(x) = x^2$



Compare each equation to the quadratic parent function. Circle all that apply.

1. y = 2(x +	$(3)^2 - 4$	2. y = $\frac{1}{2}(x - x)$	5) ² + 3
reflects		reflects	
compress	stretch	compress	stretch
moves left	moves right	moves left	moves right
moves up	moves down	moves up	moves down

"Calculate" Scratchpad:

Calculator Steps	Use
2 nd + 7 1 2 enter	Clear calculator
MATH enter enter	Convert to fraction
MATH 2 enter enter	Convert to decimal
ALPHA Y= enter	Create fraction
Up Up Enter	Copy previous work to
	make edits

"Graph" Scratchpad:

Calculator Steps	Use
2 nd GRAPH	Table
TRACE	Trace a graph to find points
2 nd TRACE 5 enter x3	Solution to a system
2 nd TRACE 2	x-intercepts
Shift left enter	
Shift right enter	
enter	
2 nd TRACE 3	Minimum of a quadratic
Shift left enter	
Shift right enter	
enter	
2 nd TRACE 4	Maximum of a quadratic
Shift left enter	
Shift right enter	
enter	

Solving Equations

Quadratic Formula (continued)



5

 $X = \{ , \}$

Quadratic Formula

Given $ax^2 + bx + c = 0$ *MUST = 0 OR = Y !!!!*

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$
3. $\frac{m}{2} - 8 = 12$
4.

Example: $4x^2 + 11x - 20 = 0$





 $x = \{ \qquad , \qquad \}$

Calculator Strategies:

- Use ALPHA Y= to create a fraction.
- Use $2^{nd} x^2$ to get $\sqrt{}$.

Solving Equations Practice

1.
$$3x - 5 = -8$$
2. $10 = 24 - 7x$ 3. $\frac{m}{2} - 8 = 12$ 4. $\frac{5}{6}x - 12 = 3$ 5. $5x + 19 = 6x + 12$ 6. $8y - 10 = 6y - 2$ 7. $x - 7 = 3x + 7$ 8. $5x - 40 = 8 - x$

9. Explain how to solve the following by hand:

$$0.5(2x-7) + x - 1 = 14 + 3(2x)$$

Solving Inequalities

Steps:	Important things to Remember:
1. Draw line 2. Box variable 3. Start moving: undo operations	 Variable must be alone before you can divide! Sign flips when diving by a negative
 Add ↔ Subtract Multiply ↔ Divide 	$<,>$ open circle \bigcirc \leq,\geq closed circle \bigcirc

Example:

 $2(x-4) \le x+3$

Practice: Solve the following & graph them on a number line.

2) 6x + 2 + 6x < 144x + 2x + 6x < 14

Attributes of Quadratic Functions (continued)

Calculator Strategy: Graph//TRACE

$y = -x^2 + 18x - 75$	$f(x) = \frac{3}{4}(x+4)^2 + 3$
Vertex:	Vertex:
Maximum or Minimum?	Maximum or Minimum?
Axis of symmetry:	Axis of symmetry:
Root(s):	Zero(s):
y-intercept:	y-intercept:

 $f(x) = x^2 - 2x - 3$ $y = -\frac{1}{4}(x-1)^2 + 4$ Vertex:Vertex:Maximum or Minimum?Maximum or Minimum?Axis of symmetry:Axis of symmetry:Solution(s):x-intercept(s):y-intercept:y-intercept:

Solving Inequalities Practice

Attributes of Quadratic Functions

		Solve follo	owing linear inequalities		
		1.	2x - 2 > 5 + 6x	2.	6y - 2 <u><</u> 2y
		3.	3x ≤ 2x + 5	4.	6x + 5 <u>></u> 4 - 4x
Vertex:	Vertex:	5.	6x - 2 < 3	6.	2x - 5 > 6x + 3
Maximum or Minimum?	Maximum or Minimum?	Solve and	l graph the solution set o	f following	
Axis of symmetry:	Axis of symmetry:	7.	8v ≥ 5	8.	$5y - 9 \le 2y + 7$
x-intercept(s):	x-intercept(s):		-,		
y-intercept:	y-intercept:	9.	5y < 8 - 7	10.	3y <u>></u> -8



Maximum or Minimum? Axis of symmetry: x-intercept(s): y-intercept:

Challenge:

$$-2(2-2x) - 4(x+5) \le -24$$

Vertex:

Intro to Functions: Function Notation

Domain & Range of Quadratics







Domain:		
Range:		

 $y=2x^2-3x-2$

Domain:

Range:

 $y=(x+3)^2+1$

Domain:

Range:

Domain:

Range:

 $f(x) = -x^2 - 7x - 6$

Domain:

Range:

 $f(x) = -\frac{1}{2}(x-4)^2 - 2$

Domain:

Range:

R:

R:

Quadratic Functions Vocabulary

Axis of symmetry: vertical line through vertex; x=____ Maximum: highest point on a parabola Minimum: lowest point on a parabola **Parabola:** shape of a quadratic function; a "u"-shape **Quadratic parent function:** $y = x^2$ **Standard Form:** $y = ax^2 + bx + c$ **Vertex Form:** $y = a(x - h)^2 + k$ Vertex: highest or lowest point of a parabola **Compression:** parabola becomes wider Stretch: parabola becomes narrower

Root/Zero/Solution: another name for x-intercept

Quadratic Formula: formula to find x-intercepts/solutions

X-intercept: point where graph crosses the x-axis (x, 0)

Y-intercept: point where graph crosses the y-axis (0, y)

Domain: x-values

Range: y-values

Intro to Functions: Function Notation Practice

Given this graph of the function f(x):

\square					
A					+
-5					5
			4	4	7
+	+	-		++	1
		5			

c. f(3) =

. .

Find:

a. f(-2) =

e. x when f(x) = 2

f. x when f(x) = 0

d. f(-5) =

x input	f(x) output
-2	3 0.56
-1	
0	j
1	
2	2



Fill in the table for the function from the given domain. f(x) = 3 - 4x

x

input

-2

-1

0

1

2

b. f(0) =

Domain & Range



Adding & Subtracting Polynomials (continued)

- 4. Simplify the following expression: 4x (2x + 5) (2x + 7)
 - a. $8x^2 + 20x + 2x + 35$
 - b. $8x^2 + 18x 7$
 - c. $6x^2 + 18x + 12$
 - d. $-8x^2 10x + 7$
- 5. Simplify the following expression: $3w(\frac{1}{2}w + 2) + 4(\frac{5}{8}w 3)$

a.
$$\frac{3}{2}w + 2 + \frac{20}{8}w - 3$$

b. $\frac{3}{2}w^2 + 6 + \frac{20}{8}w - 3$
c. $\frac{3}{2}w^2 + \frac{17}{2}w - 12$
d. $\frac{1}{2}w^2 + \frac{5}{8}w - 12$

6. Simplify the following expression: $-2(\frac{5}{2}x - 6) + 3x(\frac{1}{2}x + 4)$

a.
$$5x^2 + \frac{3}{2}x - 12$$

b. $\frac{3}{2}x^2 + 7x + 12$
c. $-\frac{3}{2}x^2 + 17x - 2$
d. $-5x^2 + 12x + 4$

- 7. Simplify the following expressions: -2f(f + 3) 8(2f + 10)
 - a. -2f² 16f
 - b. 2f² 22f 80
 - c. -2f² 22f 80
 - d. $-2f^2 + 16f + 30$

CALCULATOR STRATEGIES:

• Graph the original expression followed by each answer choice (A, B, C, D) choose the answer that is the exact same as the original graph.

Adding & Subtracting Polynomials

Adding Polynomials:

- Remove the ______ and rewrite each term.
 Combine ______. Like terms have the same
- and _____. _____

Examples:

1. $(3x^2 + 4x - 10) + (-6x^2 - 2x + 4)$

2. $(2m^2 - m) + (4m^2 + 8m - 1)$

Subtracting Polynomials:

- 1. Remove parenthesis from ______ expression and rewrite each term.
- 2. Remove the parenthesis from second expression and change each term to its ______ sign.
- 3. Combine like terms.

Examples:

1. $(4w^2 + 2w) - (6w^2 + 8w - 6)$ 2. $(3e^2 - 5e + 2) - (-10e^2 + 4e + 1)$

Domain & Range Practice:

Find the domain and Range of coordinates and decide whether it is a function.

1. (2,-3) (-5,8) (-5,6) (0,7)	Domain :	Range	Is it function ?
2. (0,-5) (-1,4.5) (-5,6.8) (0,7) Domain :	Range	Is it function ?

Find the Domain and Range for each graph.



Identify the domain and range of the function.

4.

Input	Output
1	8
3	7
5	6
7	5

Input	Output
0.4	15
0.5	13
0.6	11
0.7	9

YOUR TURN!

1.
$$(2e^2 + 3e + 10) + (-8e^2 + 11)$$
 2. $(10g^3 + g^2 - 4g) - (-2g^3 + g + 12)$

3. The area of rectangle ABCD is represented by the expression $3x^2 + 4x - 15$. The area of rectangle WXYZ is represented by the expression $8x^2 - 6x + 10$. Write an expression that represents the combined area of the rectangles.

Slope (Rate of Change)

Graph:	Table:	Ordered Pairs:
Slope Intercept Form:	Standard Form:	Point Slope Form:

Examples:



Calculator Strategies:

y= graph f(x)= graph table of values= 2^{nd} GRAPH

Convert to fraction: MATH enter enter

Fraction to Decimal: MATH 2 enter enter

Factoring-Box Method (continued)

3. $(x^2 + 2x + 3)(x - 1)$ 4. $(2x^2 + 3x + 10)(x + 2)$

5. The area of a rectangular pool is represented by the polynomial below:

 $3x^2 - 10x + 3$ What are the dimensions (length and width) of the rectangular pool?

a. (3x + 9) (x - 1)b. (x - 9) (x - 1)c. (3x - 1) (x - 3)d. (x + 10) (x + 3)

6. Which function is equivalent to $f(x) = x^2 - 2x - 15$?

a.
$$f(x) = (x - 3) (x + 5)$$

b. $f(x) = (x - 5) (x + 3)$
c. $f(x) = (3x - 1) (x + 5)$
d. $f(x) = (x + 1) (x - 15)$

Factoring-Box Method

- Label the edges of the box with the binomials
- **Write the negative and addition sign right next to the number**
- Multiply the edges to fill in the box
- Remember to use your exponent rules when MULTIPLYING only:
 - \circ x · x = x²

$$\circ x^2 \cdot x = x^3$$

- $x^4 \cdot x^2 = x^6$
- Combine the like terms
- Rewrite the terms from biggest exponent to smallest

Example: (3x - 2)(-4x + 6)



f(x) = _____

Find the area of the following polynomials: 1. (x + 2) (3x - 5) 2. (-4x + 1) (3x + 1) Parallel lines have the ______. Perpendicular lines have ______.

Parallel and Perpendicular Lines

Examples:

y = 6x - 3	y = 3x + 2	y = 3x + 9
$y = -\frac{1}{5}x + 7$	2y = 6x - 6	$y = \frac{1}{2}x - 4$
6		3

Write the slope-intercept form of an equation of the line that passes through the given point and is parallel to the graph of each equation.

(-2, 5), y = -4x + 2	(-1, -4), 9x + 3y = 8

Write the slope-intercept form of an equation of the line that passes through the given point and is parallel to the graph of each equation.

$$(3, 2), y = x + 5$$
 (-6, 4), $3y = 2x - 3$



Linear Transformations

When the slope of the line is ______than 1, the line gets _____.

When the slope of the line is ______than 1, the line gets _____.

When the y-intercept is ______, the line shifts/translates______ the parent function y=x.

When the y-intercept is ______, the line shifts/translates ______ the parent function y=x.

Examples:

Describe the change that occurs when the graph of y = x is changed to $y = \frac{1}{6}x - 2$.

Describe the change that occurs when the graph of y= 2x + 3 is transformed to $y=\frac{-1}{2}x + 3$.

If the slope of the function y = -3.5x + 12.8 is changed to 1.5, which of the following would best describe the graph of the new function?

A. The graph of the new function intercepts the y-axis at the same point as the original function

B. The graph of the new function intercepts the x-axis at the same point as the original function

C. The graph of the new function has a negative slope.

D. The graph of the new function has a positive x-intercept.

Arithmetic Sequences

 $a_n = a_1 + d(n-1)$ $a_1 = d =$

Calculator Strategy: Graph// 2nd GRAPH

The expression below describes a pattern of numbers.

0.20m + 4.50

If *m* represents the number's position in the sequence, which pattern of numbers does the expression describe? **A** 4.60, 4.70, 4.80, 4.90, 5.00 . . . **B** 6.50, 8.50, 10.50, 12.50, 14.50. . . **C** 4.70, 4.90, 5.10, 5.30, 5.50. . . **D** 4.52, 5.54, 4.56, 4.58, 4.60. . . The following table describes an arithmetic sequence, where *n* represents a number's position in the sequence.

п	1	5	8
2(n + 3)	8	16	?

Wh tab	hat is the missing value in the ple?
A	17
в	22
С	24
D	32

The first five figures in a pattern are shown below. Each figure is made up of identical circles.



If the pattern continues, which expression can be used to find the number of circles that make up Figure n?

A $n^2 + 2n$ **B** $n^2 + 2$ **C** $2n^2 + 1$ **D** $2n^2 + n$

A sequence is represented below.

Which representation is not a formula for the nth term of the sequence?

A f(x) = -20 + 15(x - 1)B $t_{ff} = -20 + (n - 1)15$ C y = 15x - 20D y = 15x - 35

Radicals

Summarize each step:

Simplify $\sqrt{27}$

 $=\sqrt{3 \cdot 3 \cdot 3}$

$$=\sqrt{(3 \cdot 3) \cdot 3}$$

$$= 3\sqrt{3}$$

Practice: Simplify each radical expression.

1. √180	2. \sqrt{18}	3. \sqrt{112}
4. 2√72	5. 6√75	6. 7√ <u>52</u>
7. $\sqrt{5} \cdot \sqrt{10}$	8. $\sqrt{15} \cdot \sqrt{10}$	9. $3\sqrt{12} \cdot \sqrt{6}$

Linear Functions Vocabulary



VOCABULARY coordinate plane coordinates diagonal line horizontal line ordered pair origin point quadrant vertical line x-axis y-axis x-coordinate y-coordinate x-intercept y-intercept

Properties of Exponents Practice

System of Linear Equations

A solution to a system of equations if where the _____, written as an

.

One Solution:	No Solution:	Infinite Solutions:
Examples:		-8x - 10y = 24 $6x + 5y = 2$
		$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

Calculator Strategies:

To find the solution from a graph: 2nd TRACE 5: intersect Enter Enter Enter Simplify the following expressions:

1.
$$(2x^{2})(4x^{3}y^{2})$$
 2. $\frac{21d^{18}e^{5}}{7d^{11}e^{3}}$ 3. $(x^{2})^{3}$
4. $x^{2/3}$ 5. x^{4} 6. $(14a^{4}b^{6})^{2}(a^{6}c^{3})^{7}$

7.
$$\frac{2y^3 \cdot 3xy^3}{3x^2y^4}$$
 8. $(2x^4y^{-3})^{-4}$ 9. $\frac{(2x^3z^2)^3}{x^3y^4z^2 \cdot x^{-4}z^3}$

Properties of Exponents

These properties are on your STAAR Chart:

PROPERTIES OF EXPONENTS	
Product of powers	$a^m a^n = a^{(m+n)}$
Quotient of powers	$\frac{a^m}{a^n} = a^{(m-n)}$
Power of a power	$(a^m)^n = a^{mn}$
Rational exponent	$a^{\frac{m}{n}} = \sqrt[n]{a^m}$
Negative exponent	$a^{-n} = \frac{1}{a^n}$

Examples: Name the property that needs to be used for each problem. (There can be more than one!)

1.
$$(2x^2)(4x^3y^2)$$
 2. $\frac{21d^{18}e^5}{7d^{11}e^3}$ 3. $(x^2)^3$

4.
$$x^{2/3}$$
 5. x^{-4} 6. $(14a^4b^6)^2(a^6c^3)^7$

7.
$$\frac{2y^3 \cdot 3xy^3}{3x^2y^4}$$
 8. $(2x^4y^{-3})^{-4}$ 9. $\frac{(2x^3z^2)^3}{x^3y^4z^2 \cdot x^{-4}z^3}$

System Word Problems

A television weighs 50 pounds and a microwave weighs 30 pounds. A TV occupies 4 cubic feet and microwave occupies 3 cubic feet. A truck is carrying 1500 pounds of cargo that occupies 138 cubic feet of space. Which system of equations can be used to find the total number of televisions, t, and microwaves, m, that are in the truck? A) 50t + 30m = 138 4t + 3m = 1500 50 + 4t = 1500 30 + 3m = 138 E) None of the above

Tickets for a movie cost \$5 for adults and \$2 for students. One afternoon 21 tickets were sold and the receipts totaled \$72. How many children tickets were bought?

The perimeter of a rectangle is 89 cm. The length is 8 cm more than the width. What is the length of the rectangle?

You and your cousin go to Wendy's for a "big" lunch. You buy 3 burgers and 2 orders of fries for \$6.50. You cousin buys 2 burgers and 5 orders of fries for \$8.00. How much did each item cost?

Linear Inequality





